

*Ollscoil na hÉireann, Gaillimh*  
*National University of Ireland, Galway*

GX910

**Semester II Examinations, 2002/2003**

Exam Code(s) 3BS1, 3BS9, 3EL1, 3EL2, 3PT1, 3PT2

Exam(s) 3<sup>rd</sup> Science

Module Code(s) EP326

Module(s) EP326: Solid State Electronics

Paper No. \_\_\_\_\_

Repeat Paper Special Paper

External Examiner(s) Professor E. Kennedy

Internal Examiner(s) Professor S. G. Jennings  
Dr. G.P. Morgan  
Dr. J. Martin

**Instructions:** Answer THREE questions.

Duration 2 hrs

No. of Answer Books \_\_\_\_\_

**Requirements:**

Handout \_\_\_\_\_

MCQ \_\_\_\_\_

Statistical Tables \_\_\_\_\_

Graph Paper \_\_\_\_\_

Log Graph Paper \_\_\_\_\_

Other Material \_\_\_\_\_

No. of Pages \_\_\_\_\_

Department(s) Experimental Physics

## EP326: Solid State Electronics

Answer THREE questions. Time allowed: TWO hours.

### Physical data for silicon at 300 K, and other constants

#### (a) Silicon at 300 K:

$N_C$	=	$2.8 \times 10^{25} \text{ m}^{-3}$	$N_V$	=	$1.04 \times 10^{25} \text{ m}^{-3}$
$\mu_n$	=	$0.14 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$	$\mu_p$	=	$0.05 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$
$D_n$	=	$36 \times 10^{-4} \text{ m}^2 \text{ s}^{-1}$	$D_p$	=	$13 \times 10^{-4} \text{ m}^2 \text{ s}^{-1}$
$n_i$	=	$1.45 \times 10^{16} \text{ m}^{-3}$	$E_G$	=	$1.12 \text{ eV}$
Relative dielectric constant, $\epsilon_s$	=	11.9			
Density of Si atoms (crystalline)	=	$5.0 \times 10^{28} \text{ atoms m}^{-3}$			
Resistivity of intrinsic Si	=	$2300 \Omega \text{ m}$			

#### (b) Other constants:

$kT$	=	$0.0259 \text{ eV}$ at $T = 300\text{K}$			
$e$	=	$1.602 \times 10^{-19} \text{ C}$	$m_e$	=	$9.11 \times 10^{-31} \text{ kg}$
$h$	=	$6.626 \times 10^{-34} \text{ J s}$	$\epsilon_0$	=	$8.85 \times 10^{-12} \text{ F m}^{-1}$
Relative dielectric constant of $\text{SiO}_2$ , $\epsilon_{\text{OX}}$	=	3.9			

Q.1 Write full notes on *TWO* of the following:

[5 marks for each part]

(a) The characteristics and behaviour of metal to semiconductor contacts.

(b) Minority carrier storage in pn junctions, and its effect on the switching speeds of diodes and bipolar junction transistors.

(c) The Haynes-Shockley experiment.

Q.2 Sketch the  $E$  vs.  $k$  relationships found in typical semiconductors, paying particular attention to the differences found between direct and indirect bandgap semiconductors.

[2 marks]

State the assumptions of the Feynman close-coupling model for electron energy states in a 1-d crystal. Give a brief quantum mechanical derivation of how this model predicts the electron energy band formula of the form

$$E = E_0 - 2A \cos(ka)$$

[4 marks]

An unperturbed atomic energy level at 5 eV is broadened into a band in a 1-d crystal which has an inter-atomic spacing  $a = 0.4 \text{ nm}$ . If the Feynman coupling coefficient for nearest-neighbour interaction is 0.5 eV, find the width of the band. Calculate the ratio of the effective mass to electron rest mass for an electron with an energy of 4.5 eV.

[4 marks]

- Q.3 By analogy with Bragg scattering of X-rays in a 1-d crystal, show that travelling wave functions for electrons in a 1-d crystal cannot exist with wavenumbers  $k = n\pi/a$ , where  $n$  is an integer, and  $a$  is the interatomic spacing. By considering the only two possible electron standing wave functions in such a 1-d crystal show that the electron energy  $E$  versus  $k$  relationship exhibits discontinuities at these  $k$  values.

[5 marks]

Sketch the general form of the  $E$ - $k$  curves in this crystal, and indicate how they confirm the band theory of electron energy. Explain briefly how this energy band theory accounts for the main qualitative features of conduction in insulators, metals and semiconductors.

[5 marks]

- Q.4 Give a brief description of a modern high-speed, drift Bipolar Junction Transistor (BJT).

[2 marks]

Sketch the excess carrier concentration under steady-state injection across the narrow base region in a npn BJT. This predicts an electron diffusion time across a uniformly-doped narrow base, with width  $W$ , given by

$$\tau_n = \frac{W^2}{2D_n}$$

In addition, sketch the majority hole concentration, charge density and built-in electric field in the base region of a typical npn drift BJT.

[2 marks]

A certain silicon npn drift BJT has a base width  $W = 1.5 \mu\text{m}$  and a minority carrier diffusion length in the base of  $53 \mu\text{m}$ . A built-in electric field exists in the base which results in a drift velocity  $v_F = 3700 \text{ m s}^{-1}$ . Find the minority carrier recombination lifetime in the base and the total base transit time. Define and estimate the transition frequency  $f_T$  for this transistor.

[5 marks]

Why are most modern high speed BJTs constructed as npn devices, rather than pnp?

[1 mark]

- Q.5 State the assumptions made in the definition of an abrupt semiconductor p-n junction. Sketch the charge density, electric field and potential variation across such a junction. Show that the depletion width,  $d_o$ , for such a junction is given by the following equation, defining all the terms used.

$$d_o = \left( \frac{2\epsilon\epsilon_o V_o}{qN} \right)^{1/2}$$

where

$$\frac{1}{N} = \frac{1}{N_A} + \frac{1}{N_D}$$

and  $V_o$  is the built-in junction barrier potential. All other terms have their usual meaning.

[6 marks]

The built in potential for such an abrupt junction, with  $N_A = 10^{22} \text{ m}^{-3}$  and  $N_D = 5 \times 10^{21} \text{ m}^{-3}$ , is found to be  $V_o = 0.678 \text{ V}$ . Find the depletion width,  $d_o$ , and the p- and n-region depletion widths,  $l_p$  and  $l_n$ , respectively at zero bias for this junction. What will the junction depletion width be if a reverse bias of  $-2 \text{ V}$  is applied to the diode?

[4 marks]